



## Supplementary Material for

### **Saturn's magnetic field revealed by the Cassini Grand Finale**

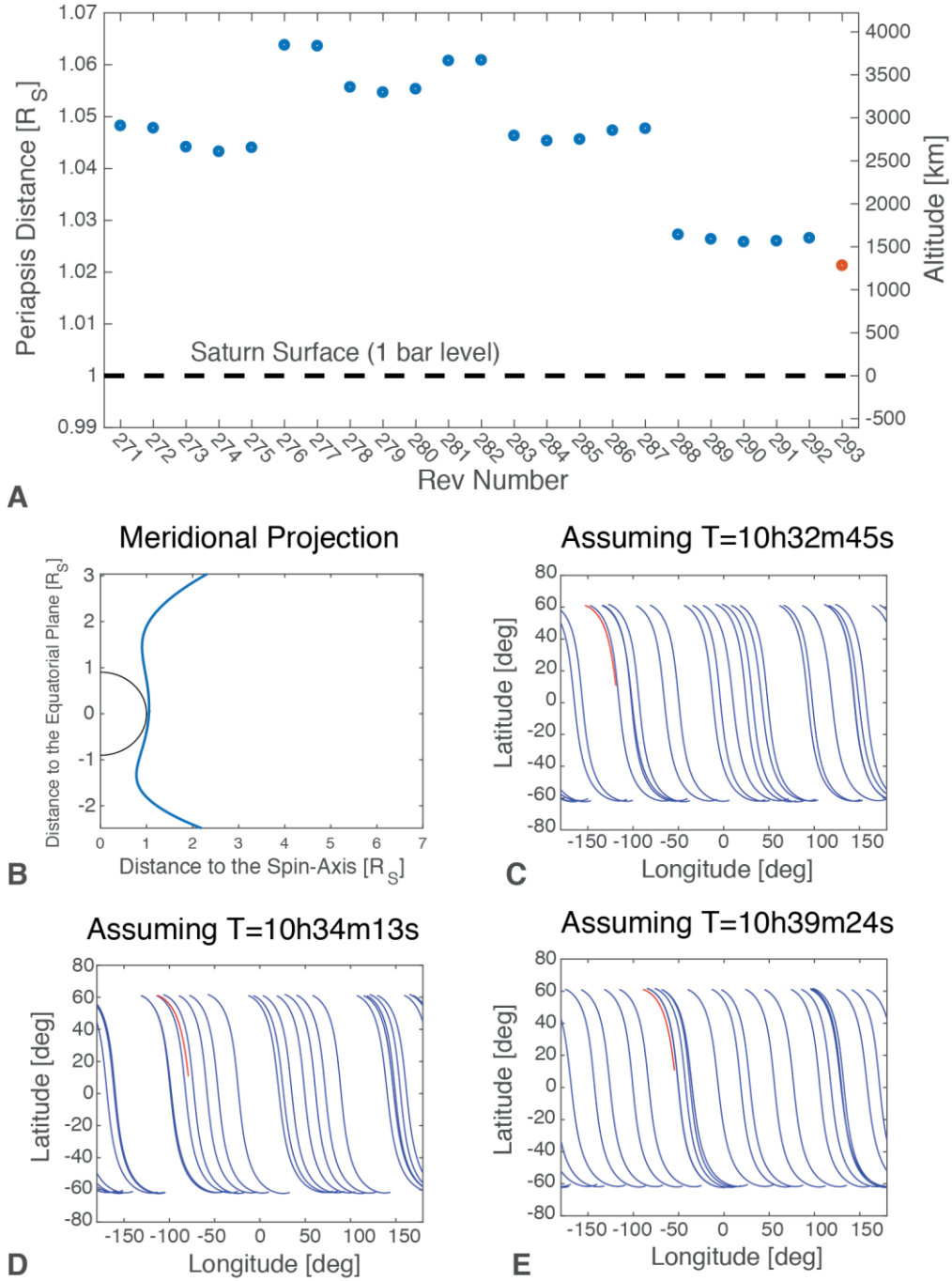
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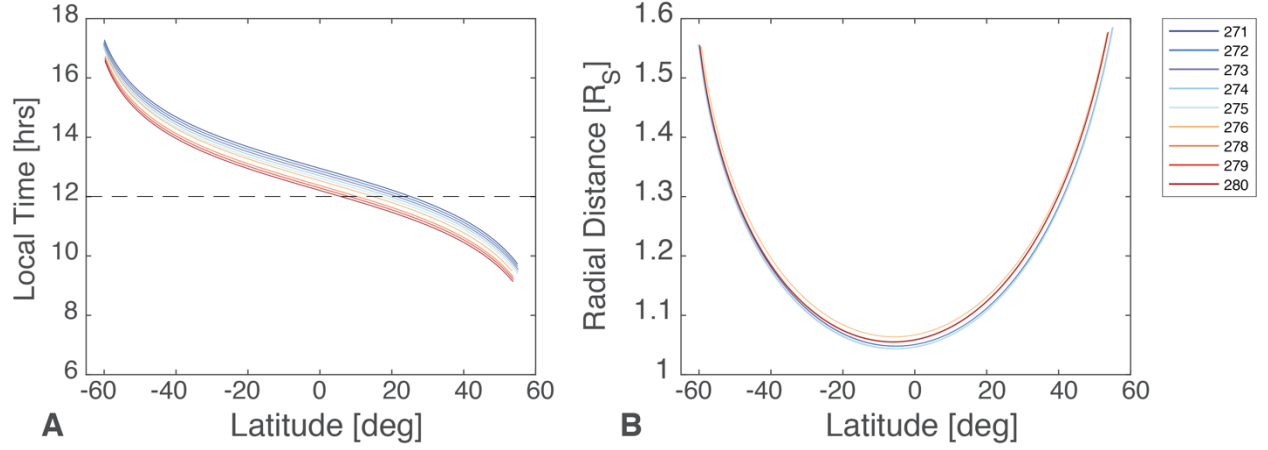
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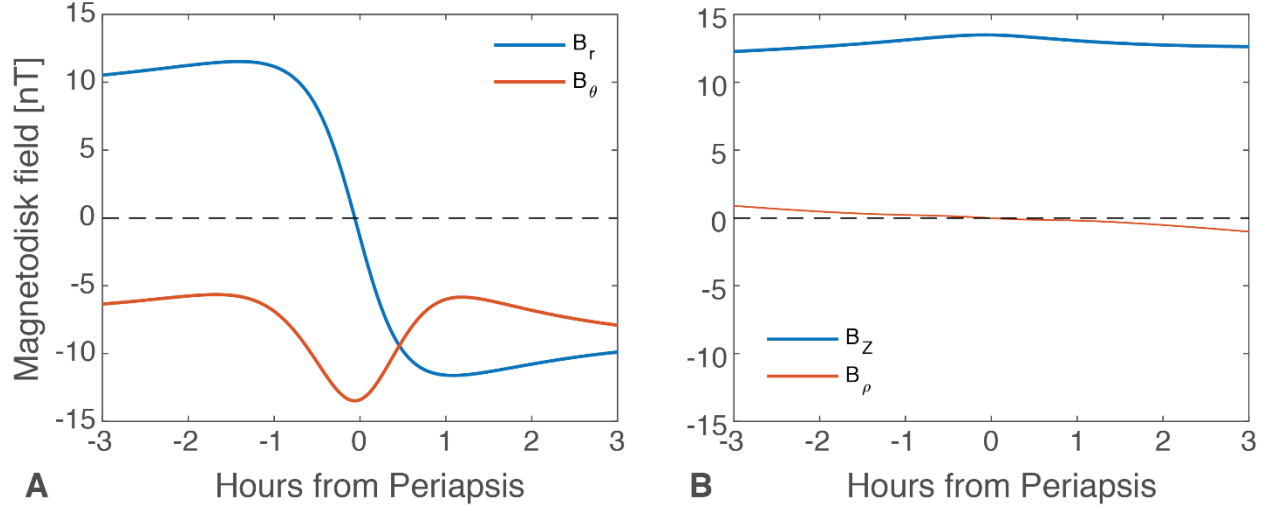
Figs. S1 to S10  
Tables S1 and S2



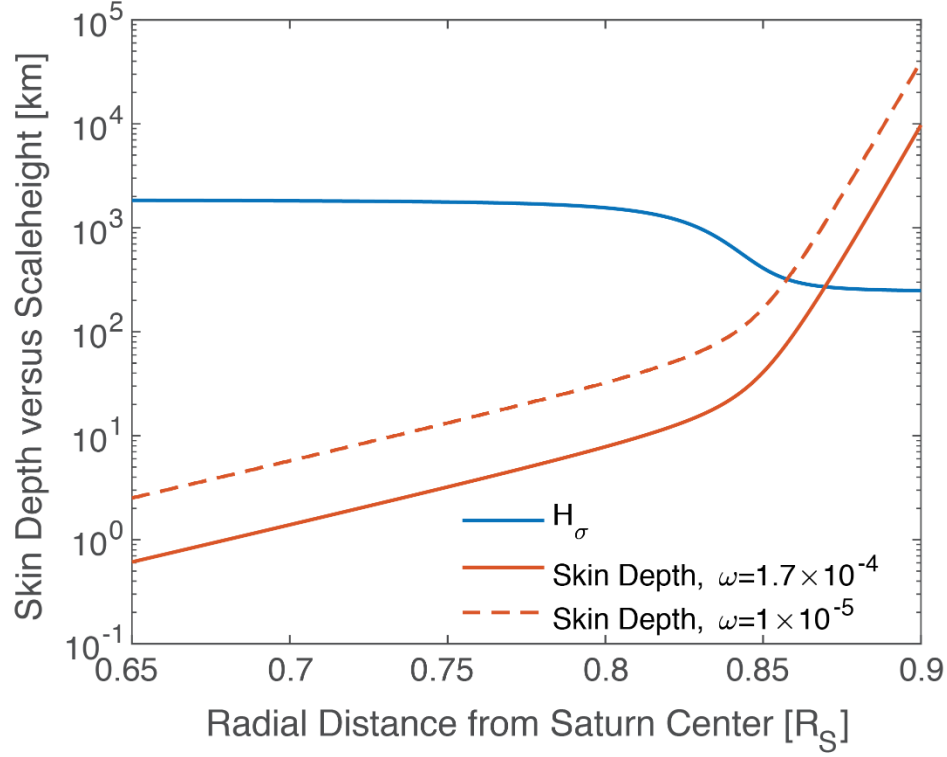
**Fig. S1. Characteristics of the trajectory of Cassini Grand Finale orbits.** Panel A shows the periapse distance for each orbit. Panel B shows the meridional projection of the first Grand Finale orbit (Rev 271). Panel C-E show and latitude-longitude coverage of the trajectory of the Cassini Grand Finale orbits for three different assumed rotation periods.



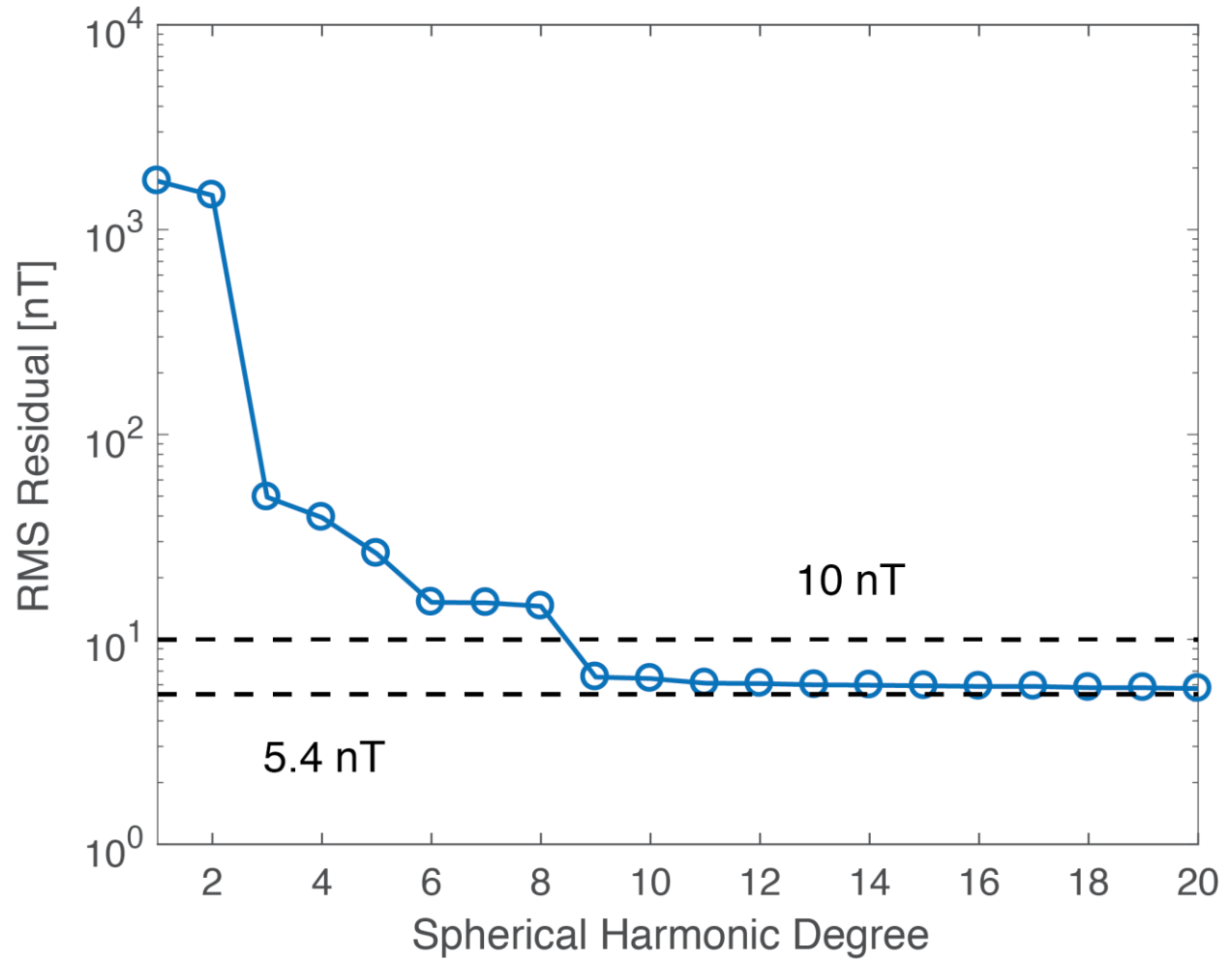
**Fig. S2. Characteristics of the trajectory of nine Cassini Grand Finale orbits.** Panel A shows local time versus latitude, while panel B shows radial distance versus latitude. The same colour code applies to both panels. We only show the portion of the trajectory when the Cassini magnetometer was in range 3 (magnetic field strength > 10,000 nT). The spacecraft was in the morning (afternoon) sector in the northern (southern) hemisphere.



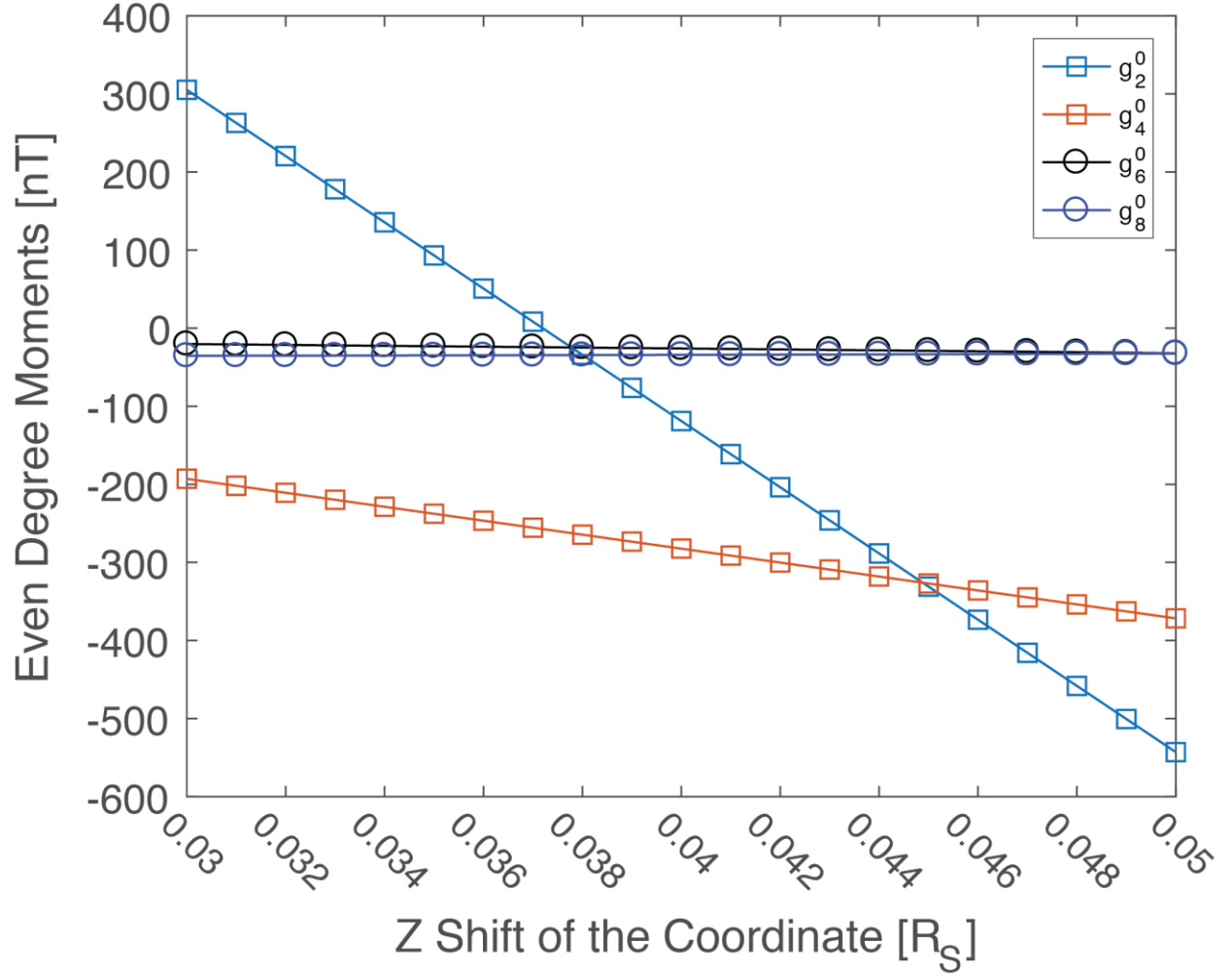
**Fig. S3. The expected magnetodisk field along the Cassini Grand Finale orbits.** The same field is shown in two different coordinate systems: Saturn-centered spherical coordinates (Panel A) and cylindrical coordinates (Panel B). The trajectory of Cassini Rev 271 was used, and the following parameters for the magnetodisk field model were adopted  $(a, b, D, \mu_0 I) = (6.5 R_S, 25 R_S, 2.5 R_S, 48.5 \text{ nT})$ . See references (22-26) for definition of the parameters of the magnetodisk field. It can be seen from the right panel that the magnetodisk field along the  $\pm 3$  hours from periapsis of the Cassini Grand Finale trajectory is close to that of a uniform field in the direction parallel to the spin-axis,  $B_z$ , around 12 nT. The expected magnetodisk field is very small in the cylindrical radial direction: less than 0.25 nT  $B_\rho$  within  $\pm 1$  hour from the periapsis. This makes  $B_\rho$  the cleanest component to probe the internal magnetic field of Saturn.



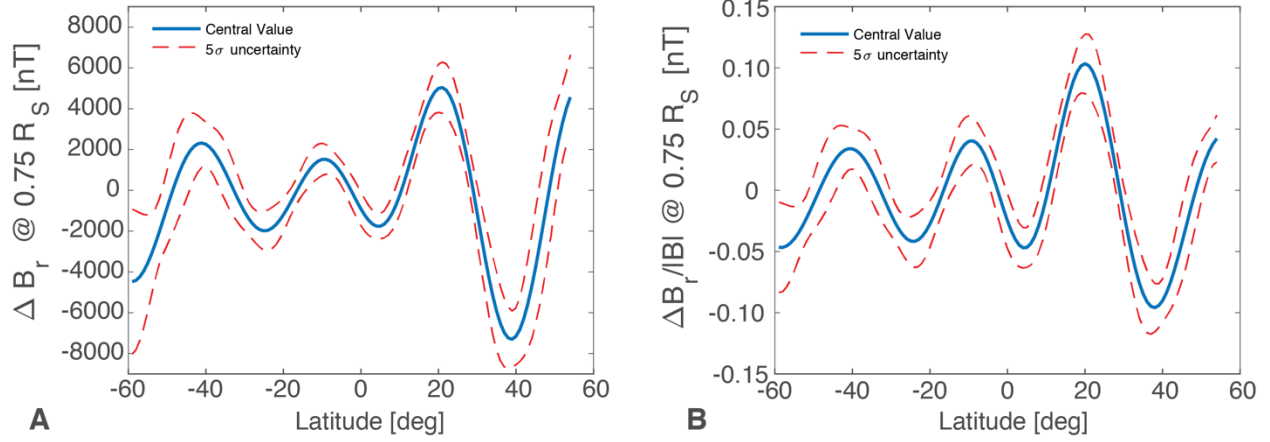
**Fig. S4. The frequency dependent electromagnetic (EM) skin depth compared to the electrical conductivity scaleheight inside Saturn.** The electrical conductivity profile of (59) is adopted for the calculations here. The two frequencies shown here correspond to the rotational frequency of Saturn  $\omega_r = \frac{2\pi}{10.5 \text{ hours}} \sim 1.7 \times 10^{-4}$  and the orbital period of Cassini Grand Finale orbits  $\omega_o = \frac{2\pi}{7 \text{ Earth days}} \sim 1.0 \times 10^{-5}$ . It can be seen that EM induction inside Saturn would occur at depth  $0.87 R_S$  for  $\omega_{ind}$  equal to the rotational frequency of Saturn and at depth  $0.86 R_S$  for  $\omega_{ind}$  equal to the orbital period of Cassini Grand Finale orbits.



**Fig. S5.** Root-mean-square (RMS) residual as a function of maximum truncation degree in unregularized inversion of Saturn's internal magnetic field from Cassini Grand Finale data. A model with Gauss coefficients up to at least spherical harmonic degree 9 is required by the data.

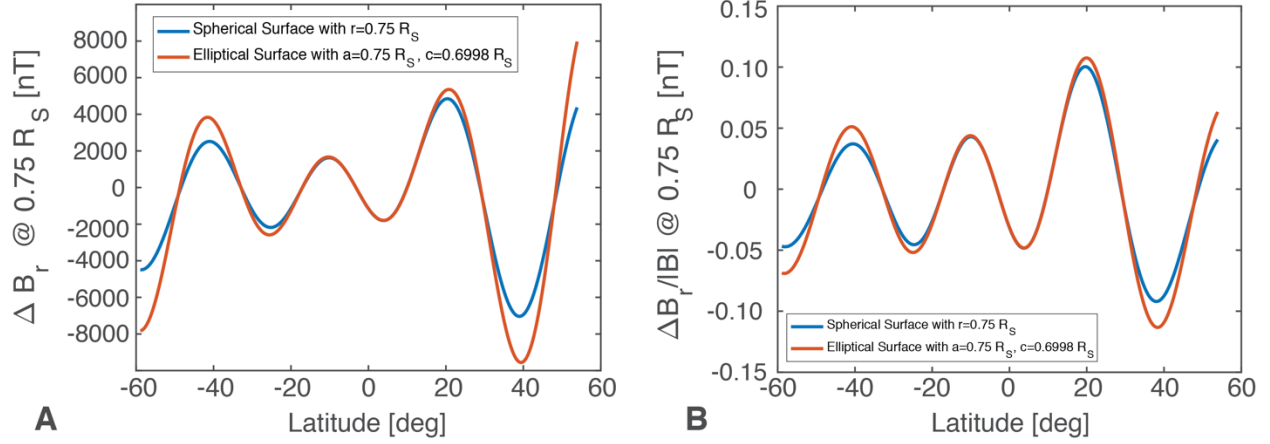


**Fig. S6. Gauss coefficients of Saturn's internal magnetic field in Z-shifted coordinates.** Only the quadrupole coefficients  $g_2^0$  becomes zero in a coordinate shifted northward by about 0.037  $R_S$ , all other even-degree moments  $g_4^0, g_6^0, g_8^0$  remain non-zero. In addition,  $g_4^0$  becomes more than an order of magnitude larger in these shifted coordinates compared to that in the Saturn-centered coordinates.

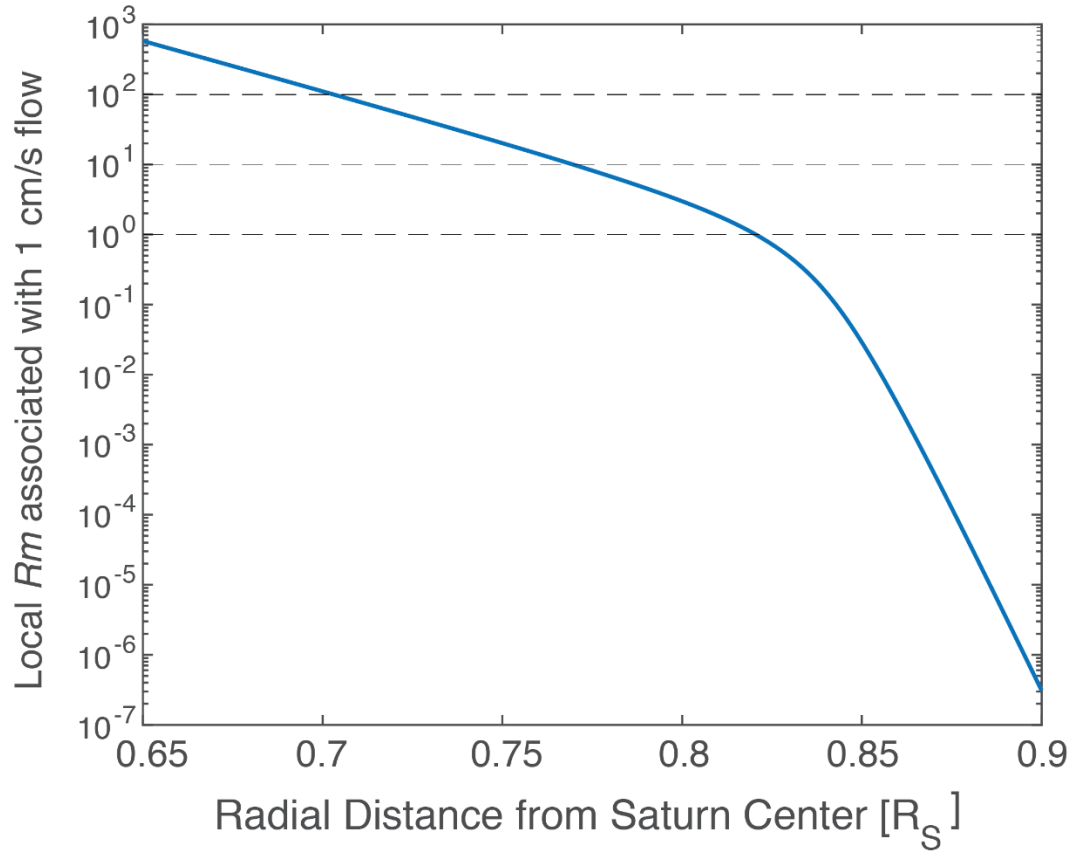


**Fig. S7. Small-scale axisymmetric magnetic field of Saturn at  $0.75 R_S$ .** Panel A shows  $\Delta B_r$  while panel B shows  $\Delta B_r/|B|$ . The central value of  $\Delta B_r$  is computed using the central values of the degree 4 to 11 Gauss coefficients of the Cassini 11 model and value of  $|B| = \sqrt{B_r^2 + B_\theta^2}$  is computed using the central values of the degree 1 to 3 Gauss coefficients of the Cassini 11 model. The uncertainties are computed using the full covariance matrix up to degree 14. The small-scale magnetic perturbations are on the order of 5-10% of the local background field.

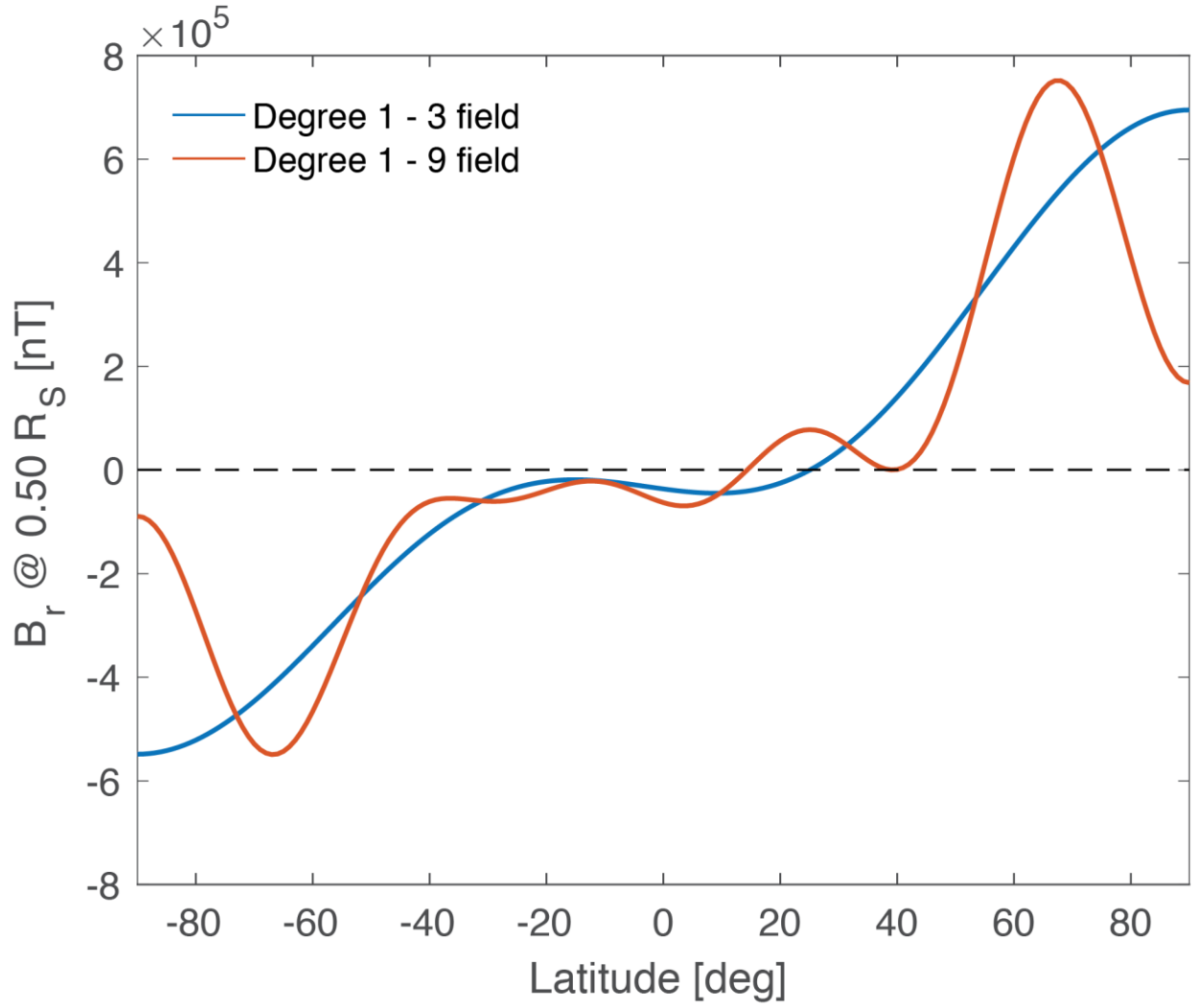




**Fig. S8. Small-scale axisymmetric magnetic field of Saturn on a spherical surface with radius  $0.75 R_S$  and on a dynamically flattened elliptical surface with equatorial radius  $0.75 R_S$  and polar radius  $0.6998 R_S$ .** Panel A shows  $\Delta B_r$  while panel B shows  $\Delta B_r/|B|$ . The central value of  $\Delta B_r$  is computed using the central values of the degree 4 to 11 Gauss coefficients of the Cassini 11 model and the value of  $|B| = \sqrt{B_r^2 + B_\theta^2}$  is computed using the central values of the degree 1 to 3 Gauss coefficients of the Cassini 11 model. It can be seen that the small-scale magnetic field are broadly similar on the spherical and dynamically flattened elliptical surface.



**Fig. S9. Local magnetic Reynolds number inside Saturn assuming 1 cm/s flow and the electrical conductivity profile of (59).**



**Fig. S10. Saturn's internal magnetic field evaluated at  $0.50 R_S$ .** The blue profile is computed from the degree 1 to degree 3 Gauss coefficients while the red profile is computed from the degree 1 to degree 9 Gauss coefficients of the Cassini 11 model (Table 1).

	Un-regularized degree 3 [nT]	Un-regularized degree 6 [nT]
$g_1^0$	21122	21156
$g_2^0$	1524	1591
$g_3^0$	2218	2296
$g_4^0$		115
$g_5^0$		74
$g_6^0$		49
RMS Residual	49.4	15.2

**Table S1. Gauss Coefficients of unregularized internal field models with different truncation degree.**

	Inner edge $a [R_S]$	Outer edge $b [R_S]$	Half thickness $D [R_S]$	$\mu_0 I$ [nT]
Nominal model	6.5	20	2.5	40
Rev 271	6.5	25	2.5	48.8
Rev 272	6.5	25	2.5	42.5
Rev 273	6.5	25	2.5	48.24
Rev 274	6.5	25	2.5	45.1
Rev 275	6.5	25	2.5	52
Rev 276	6.5	25	2.5	60
Rev 278	6.5	25	2.5	49.7
Rev 279	6.5	25	2.5	58.1
Rev 280	6.5	25	2.5	29.9

Table S2. Coefficients of the magnetodisk field model derived for each orbit.

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